

## GRAND TEST-2

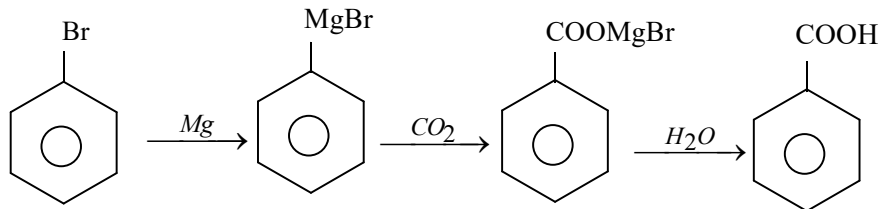
Max Marks : 360

SOLUTIONS

## CHEMISTRY

1. Volume strength =  $5.6 \times \text{Normality}$ 

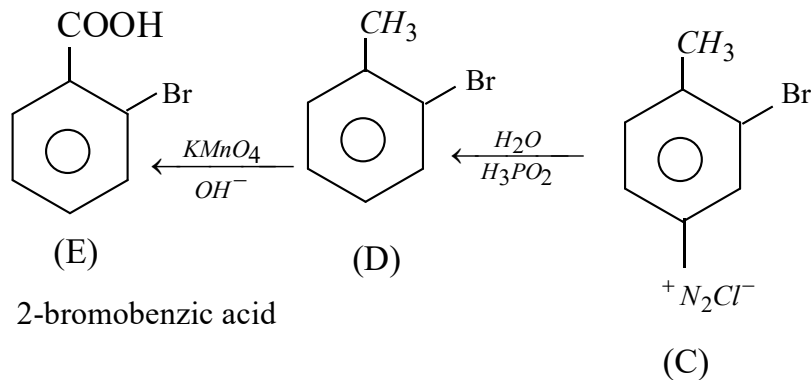
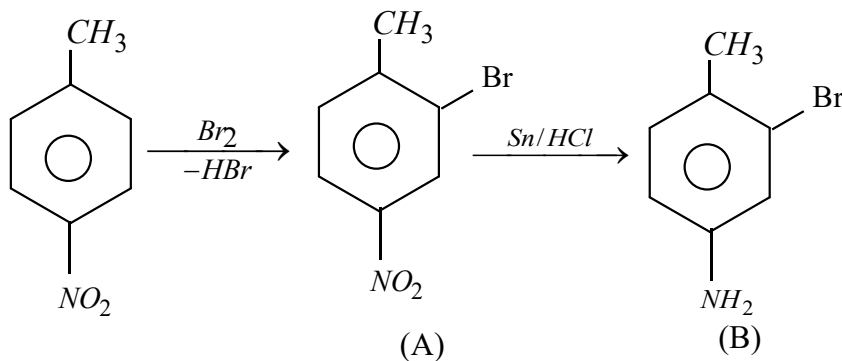
2.

3.  $5f^{14}, 6d^3 \Rightarrow \text{Total } 17e^-$ 

$$5f^{14} = (n+l) = 5+3 = 8$$

$$6d^3 = (n+l) = 6+2 = 8$$

5.



2-bromobenzoic acid

$$6. \quad \bar{V}_{H_2} = \bar{V}_{He^+} \Rightarrow \frac{1}{\lambda_{H_2}} = \frac{1}{\lambda_{He^+}}$$

$$R \left( \frac{1}{n_1^2} - \frac{1}{n_2^2} \right) = RZ^2 \left( \frac{1}{2^2} - \frac{1}{4^2} \right)$$

$$\therefore n_1 = 1 \text{ \& } n_2 = 2$$

9. Vender wall's equation for 1 mole gas is  $\left( p + \frac{a}{v^2} \right) (v-b) = RT$ AT low p, volume is High. so  $(V-b)=V$

$$\therefore \left( p + \frac{a}{V^2} \right) v = RT$$

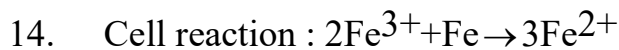
$$\text{(or) } PV + \frac{a}{V} = RT$$

$$\therefore PV = RT - \frac{a}{V}$$

$$10. \text{ Work done} = \frac{1}{2}(4P_1 - P_1)(3V_1 - 2V_1) \\ = 3 P_1 V_1$$

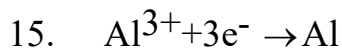
$$12. \text{ Given } \frac{\Delta T_{fA}}{\Delta T_{fB}} = \frac{2}{1} = \frac{1}{1/2} \therefore e$$

B should associate to show **lower in**  $\Delta T$



$$E_{cell}^0 = 0.77 - (-0.44) = +1.21 \rightarrow \text{spontaneous}$$

$\Rightarrow \therefore \text{Fe}^{3+}$  &  $\text{Fe}$  will reduce



$$1 \text{ mol Al} = 27\text{g} = 3F$$

$$13.5 \text{ gr of Al} = ? \quad F = 1.5F$$

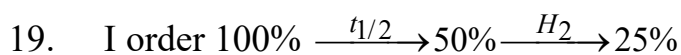
$$17. \text{ Order with respect to A } \left[ \frac{0.03}{0.01} \right]^x = \frac{45}{5}$$

$$3^x = 3^2 \quad x = 2$$

$$\text{Order with respect to B } \left( \frac{0.02}{0.01} \right)^y = \frac{5}{2.5}$$

$$2^y = 2^1 \quad y = 1$$

$$\text{Rate} = K[A]^2[B]^1$$



$$\text{Given } 2t_{1/2} = 1\text{hr}$$

$$\therefore t_{1/2} = \frac{1}{2}\text{hr}$$

$$20. \%N = \frac{28 \times V_{N_2 \text{ at STP}} \times 100}{22400 \times W_{oC}}$$

$$= \frac{28 \times 22.4 \times 100}{22400 \times 0.25} = 11.2\%$$

24. It is a basic buffer

$$\text{pH} = 8.65$$

$$\therefore \text{pOH} = 14 - 8.65 = 5.35$$

$$\text{pOH} = p^{kb} + \log \frac{[\text{NH}_4^+]}{[\text{NH}_4\text{OH}]}$$

$$5.35 = 4.75 + \log \frac{[\text{NH}_4^+]}{[\text{NH}_4\text{OH}]}$$

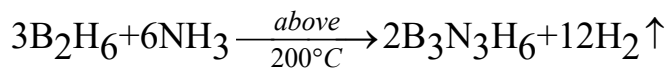
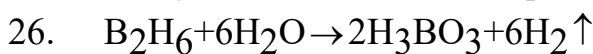
$$\therefore \frac{[\text{NH}_4^+]}{[\text{NH}_4\text{OH}]} = \text{anti log}(5.35 - 4.75)$$

$$\approx 4$$

$$\therefore \frac{[\text{NH}_4^+]}{[\text{NH}_4\text{OH}]} = \frac{0.2 \times 30}{0.3 \times V_1} = 4$$

$$\therefore V = 5 \text{ ml}$$

25. 1°-alkyl halides follows  $\text{SN}^2$  path and walden Inversion takes place

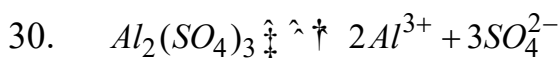


$$\therefore K_{sp} = 108x^5$$

28.  $4 \times 58.5 \text{ g}$  - No. of unit cells =  $6 \times 10^{23}$

1 gram = ?

$$= \frac{1}{4 \times 58.5} \times 6 \times 10^{23} = 2.56 \times 10^{21}$$



Initially let	1	0	0
After	1 - $\alpha$	2 $\alpha$	3 $\alpha$

$$i = \frac{1 - \alpha + 2\alpha + 3\alpha}{1} = 4.2$$

$$\Rightarrow 1 + 4\alpha = 4.2$$

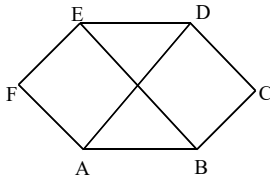
$$\Rightarrow 4\alpha = 3.2 \Rightarrow \alpha = \frac{3.2}{4} = 0.8 = 80\%$$

## MATHEMATICS

31.  $T_{r+1} = 100c_r (5^{1/6})^{100-r} (2^{1/8})^r$  As 5 and 2 are relatively prime,  $T_{r+1}$  will be rational if  $\frac{100-r}{6}$  and  $\frac{r}{8}$  are both integers  $\Rightarrow 100-r$  is a multiple of 6 and  $r$  is a multiple of 8,  $100-r$  is multiple of 6 if  $r = 4, 12, 20, \dots, 100$  of which 12, 36, 60, 84 are divisible by 6. Hence, there are just four rational terms.  $\Rightarrow$  no. of irrational terms is  $101 - 4 = 97$ .
32.  $Z = re^{i\theta}$  Then  $\frac{r^2}{12}(e^{i\theta} + e^{-i\theta})^2 = 1 - \frac{r^2}{3}$   
 $\Rightarrow \frac{r^2 \cos^2 \theta}{3} = \frac{3-r^2}{3} \Rightarrow r^2 = \frac{3}{1+\cos^2 \theta} \leq 3$  max value of  $|z| = r = \sqrt{3}$
33. If the lines  $a_1x + b_1y + c_1 = 0$  and  $a_2x + b_2y + c_2 = 0$  meets the axes is concyclic points then  $a_1a_2 = b_1b_2$
34. **Sol :** A  $(x_1, y_1)$  be any point on parabola  $y^2 = 4x$  and B  $(h, k)$  is its image w.r.t  $x-y+13 = 0$  then  $\frac{h+x_1}{2} - \frac{k+y_1}{2} + 13 = 0$  and  $\left(\frac{k-y_1}{h-x_1}\right)(1) = -1 \Rightarrow x_1 = h-13, y_1 = -k+13$   
 $\therefore (h+13)^2 = 4(k-13)$
35. Formula application
36. Taking the coordinates of vertices O, P, Q, R as  $(0,0), (a,0), (a,a), (0,a)$  respectively we get the coordinates of M as  $\left(a, \frac{a}{2}\right)$  and of N as  $\left(\frac{a}{2}, a\right)$
37. Area =  $\frac{|c|}{2\sqrt{h^2-ab}}$
38. Shortest distance is 0.
39. foot of the perpendicular A  $(1,0,2)$  to the line is  $B\left(\frac{1}{2}, 1, -3/2\right)$
40. we find  $\frac{dx}{dt}$  when  $x = \frac{1}{2}$  and  $y = \frac{\sqrt{3}}{2}$  given that  $\frac{dy}{dt} = -3$  units/s and  $x^2 + y^2 = 1$   
 Differentiating  $x^2 + y^2 = 1$ , we have  $2x\frac{dx}{dt} + 2y\frac{dy}{dt} = 0$   
 Putting  $x = \frac{1}{2}, y = \frac{\sqrt{3}}{2}$  and  $\frac{dy}{dt} = -3$ , we have  $\frac{1}{2}\frac{dx}{dt} + \frac{\sqrt{3}}{2}(-3) = 0 \Rightarrow \frac{dx}{dt} = 3\sqrt{3}$
41. Let  $f(x) = x^2 - 2ax + a^2 + a - 3 = 0$   
 Then (i)  $\Delta \geq 0$  (ii) sum of root  $< 6$  (iii)  $f(3) > 0$
42.  $b = \frac{2ac}{a+c}; c = \frac{2bd}{b+d} \therefore (a+c)(b+d) = \frac{2ac}{b} \cdot \frac{2bd}{c} = 4ad \Rightarrow ab + bc + cd + ad = 4ad$
43.  $\sqrt{\frac{\sum_{i=1}^x x_i^2}{n}} = \sqrt{\frac{400}{n}} \geq \frac{80}{n} \Rightarrow n \geq 16$  hence, possible value of  $n = 18$ .
44.  $\cot \theta + \tan \theta = m \Rightarrow \sec^2 \theta = m \tan \theta - (1)$   
 $\sec \theta - \cos \theta = n \Rightarrow \tan^2 \theta = n \sec \theta - (2) \quad \tan^2 \theta = n(nm^2)^{1/3}$   
 from (1) & (2)  $\Rightarrow$  similarly  $\sec^2 \theta = m(n^2m)^{1/3}$  eliminate  $\theta$

45.  $\sin^{-1}(\sin 3) = \pi - 3$      $\sin^{-1}(\sin 4) = \pi - 4$      $\sin^{-1}(\sin 5) = 5 - 2\pi$      $sum = -2$

46. 
$$\left. \begin{array}{l} AD = 2BC \Rightarrow x = 2 \\ CF = 2BA \Rightarrow y = 2 \end{array} \right\} \Rightarrow xy = 4$$



47. for no solution or infinitely many solutions

$$\begin{vmatrix} \alpha & -1 & -1 \\ 1 & -\alpha & -1 \\ 1 & -1 & -\alpha \end{vmatrix} = 0 \Rightarrow (\alpha - 1)^2(\alpha + 2) = 0 \Rightarrow \alpha = 1, 1, -2$$

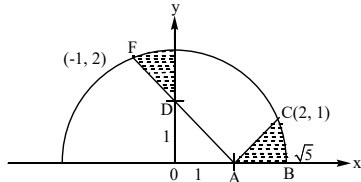
but for  $\alpha = 1$ , there are infinite solutions when  $\alpha = -2$ , we have

$-2x - y - z = 3$ ,     $x + 2y - z = -3$      $x - 2y + 2z = -3$  adding  $0 = -9$ , which is not true  $\Rightarrow$  no solution.

48.  $AA' = I$

$$\Rightarrow \begin{pmatrix} \lambda & 0 & \lambda \\ \lambda & 0 & -\lambda \\ 0 & 1 & 0 \end{pmatrix} \begin{pmatrix} \lambda & \lambda & 0 \\ 0 & 0 & 1 \\ \lambda & -\lambda & 0 \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$\Rightarrow \begin{pmatrix} 2\lambda^2 & 0 & 0 \\ 0 & 2\lambda^2 & 0 \\ 0 & 0 & 1 \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$



49.

The two shaded areas are congruent

Area = The area ACEF

$$= \frac{1}{4}(\text{area of circle}) - \Delta OAD$$

$$= \frac{5\pi}{4} - \frac{1}{2} = \frac{5\pi - 2}{4}$$

50. Differentiating  $x^2 + 2y^2 - y = c$ ,  $2x + 4yy_1 - y_1 = 0 \rightarrow 2x = -(4y - 1)y_1$

Replacing  $y$  by  $-\frac{1}{y_1}$ ,  $\frac{2xdy}{dx} = 4y - 1$

$$\int \frac{4dy}{4y - 1} = \int \frac{2dx}{x}$$

$$\ln(4y - 1) = \ln x^2 + \ln c_1$$

$$4y - 1 = c_1 x^2$$

$$y = cx^2 + \frac{1}{4}, 4c = c_1$$

51. Clearly  $\lim_{x \rightarrow 0} x e^{-\frac{e-1}{x} + \frac{1}{x^2}} = 0 = f(0)$  Continuous at  $x = 0$

$$\text{Let } \lim_{x \rightarrow 0^-} \frac{f(x) - f(0)}{x - 0} = \lim_{x \rightarrow 0^-} \frac{x e^{-\frac{1}{x}} - 0}{x - 0} = 1$$

$$\lim_{x \rightarrow 0^+} \frac{f(x) - f(0)}{x - 0} = \lim_{x \rightarrow 0^+} \frac{x e^{-\frac{1}{x}} - 0}{x - 0} = \lim_{x \rightarrow 0^+} e^{-2/x} = 0$$

Not differentiable at  $x = 0$

52.  $\frac{1}{\alpha}, \frac{1}{\beta}$  are the roots of  $cx^2 + bx + a = 0$

$$cx^2 + bx + a = c \left( x - \frac{1}{\alpha} \right) \left( x - \frac{1}{\beta} \right)$$

53. T :  $x - x = 0$  is integers reflexives  $y - x$  is integer symmetric  $(x-y) + (y-z) = x - z$  is integers transitive  $\therefore$  T is equivalence and S :  $y - x = 1 \Rightarrow x - x \neq 1$  not reflexive.

54.  $\int_{-\pi}^{\pi} \frac{\cos^2 x}{1+a^x} dx = \int_0^{\pi} \left[ \frac{\cos^2 x}{1+a^x} + \frac{\cos^2(-x)}{1+a^{-x}} \right] dx$   
 $= \int_{-\pi}^{\pi} \cos^2 x dx = 2 \int_0^{\pi/2} \cos^2 x dx = \frac{\pi}{2}$

55.  $\int_{\pi}^{2\pi} [2 \sin x] dx = \int_{\pi}^{6\pi/6} (-1) dx + \int_{7\pi/6}^{3\pi/2} (-2) dx + \int_{3\pi/2}^{11\pi/6} (-2) dx + \int_{11\pi/6}^{2\pi} (-1) dx$

56.  $\frac{dy}{dx} = \frac{x^2 + xy + y^2}{x^2}$  is a homogeneous differential equation, put  $y = vx$ .

57. We have  $\int e^x \cos x dx = \frac{1}{2} e^x (\sin x + \cos x)$

Therefore,  $I = x \cdot \frac{1}{2} e^x (\sin x + \cos x) - \frac{1}{2} \int e^x (\sin x + \cos x) dx + \int e^x \sin x dx$

$$= \frac{x}{2} e^x (\sin x + \cos x) - \frac{1}{2} \int e^x (\cos x - \sin x) dx$$

$$= \frac{x}{2} e^x (\sin x + \cos x) - \frac{1}{2} [e^x \cos x] + c$$

$$= \frac{1}{2} e^x (x \sin x + x \cos x - \cos x) + c$$

58. from truth table  $p \rightarrow (q \rightarrow p) \approx p \rightarrow (p \vee q)$

59. We have  ${}^{100}C_{50} = \frac{100!}{50!50!}$

The exponent of 7 in 50! is  $\left[ \frac{50}{7} \right] + \left[ \frac{50}{7^2} \right] = 7 + 1 = 8$

And the exponent of 7 in 100! =  $\left[ \frac{100}{7} \right] + \left[ \frac{100}{7^2} \right] = 14 + 2 = 16$ ,

Thus, exponent of 7 in  ${}^{100}C_{50}$  is  $16 - 2(8) = 0$

60. total no of ways of answering is 15. Out of 15 combinations only **one** is correct. The probability of ticking the answer at the first .. is  $\frac{1}{15}$ , that of 2<sup>nd</sup> is  $\frac{14}{15} \cdot \frac{1}{14} = \frac{1}{15}$  and that of

third is  $\frac{14}{15} \cdot \frac{13}{14} \cdot \frac{1}{13} = \frac{1}{15} \therefore$  probability that the student will get marks for the question if

he is allowed into 3 chances  $= 3 \left( \frac{1}{15} \right) = \frac{1}{5}$ .

**PHYSICS**

61.  $V_m = 3i$

Let  $V_R = ai + bj$

$V_{RM} = \overline{V_R} = \overline{V_m}$

$= 3i - (ai + bj)$

$V_{RM} = (3 - a)i + bj$

$V_{RM}$ . Vertical

i.e  $3 - a = 0$

$a = 3$

If  $V_m = 6i$

$V_{RM}^1 = 6i - (ai + bj)$

$V_{RM}^1 = (6 - a)i - bj$

It is  $45^\circ$  with vertical

i.e,  $6 - a = b$

$6 - 3 = b$

$b = 3$

$VR = 3i + 3j$

$|VR| = 3\sqrt{2} \text{ kmph}$

62. Given  $\frac{V^2}{R} = 36$

$V^2 = 36 \cdot 9 ; V = 18V$

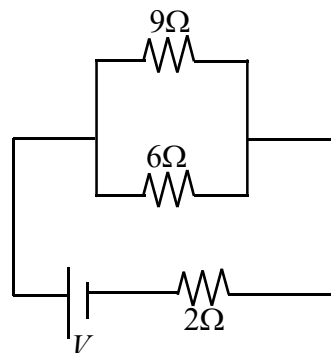
Equivalent of 6W & 9W

$\frac{6 \cdot 9}{15} = \frac{18}{5} = 3.6W$

3.6W and 2W

Are in series

So  $V \propto R$   $\frac{V_1}{V_2} = \frac{R_1}{R_2}$



$$\frac{18}{V_2} = \frac{3.6}{2}$$

$$V_2 = 10V$$

63.  $x = 3t^2 - t^3$

When x is maximum  $\frac{dx}{dt} = 0$

$$\frac{dx}{dt} = 6t - 3t^2 = 0 \quad \text{so maximum } x \text{ @}$$

$$6t = 3t^2 \quad x = 3 \cdot 4 - 8$$

$$3t = 6 \quad = 4m$$

$$t = 2$$

$$x = 0. 3t^2 = t^3$$

$$t = 3 \text{ sec}$$

When  $t = 4 \text{ sec}$

$$x = 3 \cdot 16 - 64 = -16m$$

So distance travel .  $4 + 4 + 16 = 24m$

64.  $P = 1000kw = 10^3 \cdot 10^3 J / \text{sec}$

$$\text{Energy in one hour} = 10^6 \cdot 3600J$$

$$36 \cdot 10^8 J$$

$$\text{mass decay} = \frac{E}{C^2} = \frac{36 \cdot 10^8}{9 \cdot 10^{16}}$$

$$= 4 \cdot 10^{-8} \text{ kg} = 40mg$$

65. PE at the top of the inclined plane

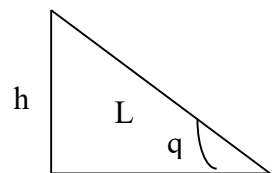
= work done against friction

$$mgh = \frac{m}{2} mg \frac{L}{3} \cos q + mg \frac{L}{3} \cos q$$

$$h = \frac{mL \cos q}{3} \left( \frac{1}{2} + 1 \right)$$

$$\frac{h}{L} = \frac{m}{3} \cos q \cdot \frac{3}{2}$$

$$\sin q = \frac{m \cos q}{2} \quad m = 2 \tan q$$



66.  $\frac{E}{l} \cdot \frac{l}{5} = \frac{E}{3l/2} \cdot l$



$$\frac{l}{5} = \frac{2}{3}l^1$$

$$l^1 = \frac{3l}{10}$$

67.  $F = ks^{-1/3}$

$$m \frac{dJ}{dt} = ks^{-1/3}$$

$$m \frac{dJ}{ds} \frac{ds}{dt} = ks^{-1/3}$$

$$m \frac{dJ}{ds} J = ks^{-1/3} ds$$

$$m \frac{J^2}{2} = \frac{ks^{2/3}}{2/3}$$

$$J \propto s^{1/3}$$

$$P = FV$$

$$P \propto s^{-1/3} s^{1/3}$$

$$P \propto s^0$$

68.  $\frac{8q}{x^2} = \frac{2q}{(x-L)^2}$

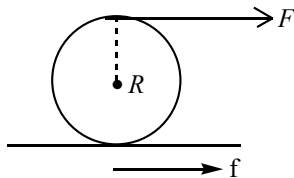
$$\frac{2}{x} = \frac{1}{x-L}$$

$$2x - 2L = x$$

$$x = 2L$$

69.  $F + f = Ma$  Ⓜ translational motion

$$FR - fR = Ia = I \frac{a}{R} \text{ Rotational motion}$$



$$F - f = \frac{Ia}{R^2} \text{ Ⓜ (1) } \quad I = \frac{2}{5}MR^2$$

$$F + f = Ma \text{ Ⓜ (2)}$$

Solving

$$a = \frac{10F}{7M}$$

70. Mean square value  $\frac{\int_0^{T/4} v^2 dt}{\int_0^{T/4} dt}$

For  $\frac{T}{4}$

$v = at$  ( up to  $T/4$  increases with time)

At  $t = T/4, V = v_0$

$$v_0 = \frac{aT}{4}$$

$$a = \frac{4v_0}{T}$$

$$ms = \frac{\int_0^{T/4} v^2 dt}{\int_0^{T/4} dt} = \frac{\int_0^{T/4} a^2 t^2 dt}{\int_0^{T/4} dt}$$

$$= \frac{16v_0^2 \int_0^{T/4} t^2 dt}{T^2 \cdot T/4}$$

$$= \frac{V_0^2}{3}$$

$$v_{rms} = \frac{v_0}{\sqrt{3}}$$

71.  $f = at - at^2$

$$\frac{df}{dt} = e = at - 2at$$

$$H = \int_0^t P dt = \int_0^t \frac{e^2}{R} dt$$

$$H = \frac{1}{R} \int_0^t (at - 2at)^2 dt$$

$$= \frac{1}{R} \int_0^t a^2 t^2 + \frac{4a^2 t^3}{3} - 4a^2 t \cdot t^2 dt$$

$$= \frac{1}{R} \int_0^t a^2 t^2 + \frac{4}{3} a^2 t^3 - 2a^2 t^3 dt$$

$$= \frac{a^2}{R} \int_0^t t^2 + \frac{4}{3} t^3 - 2t^3 dt$$

$$= \frac{a^2}{R} \left[ \frac{t^3}{3} + \frac{4}{12} t^4 - \frac{2}{4} t^4 \right]$$

$$= \frac{a^2}{3R} t^3$$

72. In FM Band width is less

73.  $B = \frac{m\omega i}{2r} = \frac{m_b e}{2r T}$

$$T a r^{3/2}$$

$$B a \frac{1}{r^{3/2}} a \frac{1}{r^{5/2}}$$

$$r a n^2$$

$$B a \frac{1}{n^5}$$

74. Voltage gain =  $A_v = \frac{v_0}{V_{in}} = \frac{D I_c R_o}{D I_b R_i}$

$$\frac{5mA \ 6kW}{50mA \ 600W}$$

=1000

75. After two hours  $x : y = \frac{No}{2} : \frac{No}{2} = 1:1$

Four hours  $= \frac{No}{4} : \frac{3No}{4} = 1:3$

Six hours =  $\frac{No}{8} : \frac{7No}{8} = 1:7$

Here it is 1 : 4

So t > 4 hrs < 6 hrs

76. If  $u = x$

$$J = 10 + x$$

$$f = 12cm$$

$$\frac{1}{u} + \frac{1}{n} = \frac{1}{f}$$

$$\frac{1}{x} + \frac{1}{10+x} = \frac{1}{12} \text{ ® solving}$$

$$u = x = 20cm$$

$$J = 30$$

$$M = 1 - 5$$

$$M = v/u = 1.5$$

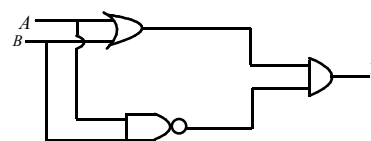
77.  $Y = (A + B)(\overline{AB})$

$$= (A + B)(\overline{A} + \overline{B})$$

$$= A\overline{A} + \overline{A}B + A\overline{B} + B\overline{B}$$

$$= 0 + \overline{A}B + A\overline{B} + 0$$

$$= \overline{A}B + A\overline{B} = \text{' OR gate'}$$



78.  $dQ = mSdT$

$$\begin{aligned} \int_0^{20} dQ &= mA \int_0^{20} T^3 dt \\ &= mA \left[ \frac{T^4}{4} \right]_0^{20} \\ &= \frac{mA}{4} (20)^4 = \frac{mA}{4} \cdot 16 \cdot 10^4 = 4mA \cdot 10^4 \end{aligned}$$

79.  $h\nu = R \frac{hc}{\lambda} \left[ \frac{1}{(n-1)^2} - \frac{1}{n^2} \right]$

$$R \frac{hc}{\lambda} \frac{n^2 - n^2 + 2n - 1}{n^2(n-1)^2} \text{ if } n \gg 1$$

$$= \frac{R \cdot 2n}{n^4} = \frac{1}{n^3}$$

80. Initial internal energy =  $4(Cv)_{dia} \cdot T = 4 \cdot \frac{5R}{2} T$

final internal energy =  $2(Cv)_{dia} T + 4(Cv)_{mono} T$

$$2 \cdot \frac{5R}{2} T + 4 \cdot \frac{3R}{2} T$$

$$= 11RT$$

Then  $Q = 11RT - 10RT = RT$

81. Equation of the particles are

$$x_1 = A \sin \left( \frac{2\pi}{\lambda} wt + \frac{p}{6} \right)$$

$$x_2 = A \sin \left( \frac{2\pi}{\lambda} wt + \frac{p}{6} \right)$$

When they meet  $A \sin \left( \frac{2\pi}{\lambda} wt + \frac{p}{6} \right) = -A \sin \left( \frac{2\pi}{\lambda} wt + \frac{p}{6} \right)$

$$2A \sin \left( \frac{2\pi}{\lambda} wt + \frac{p}{6} \right) = 0 \qquad \omega t + \frac{\pi}{6} = \pi$$

$$\omega t = \frac{5\pi}{6}$$

$$t = \frac{5\pi}{6\omega} = \frac{5\pi T}{6 \cdot 2\pi} = \frac{5T}{12}$$

Altier

$$- \frac{A}{2} \text{ to } A \text{ @ } \frac{T}{6}$$

They meet at the mean position

$$-A - A \otimes 0 = \frac{T}{4} \text{ so } \frac{T}{4} + \frac{T}{6} = \frac{5T}{12}$$

82. No. of beats  $\frac{20}{2} = 10$

If tuning fork frequency is n.

$$\frac{n+10}{n-10} = \frac{10.2}{9.2} \left( n \propto \frac{1}{l} \right)$$

$$n = 194 \text{ Hz}$$

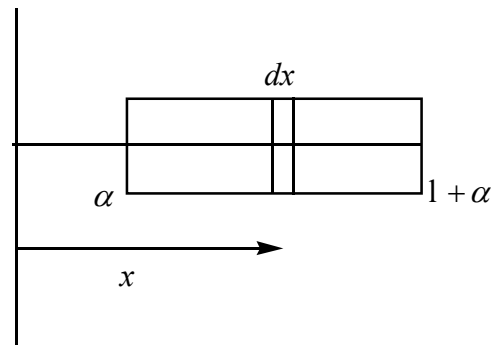
83.  $dF = \frac{Gm \cdot l \, dx}{x^2}$

$$dF = \frac{Gm(a + bx^2)dx}{x^2}$$

$$F = Gm \int_a^{l+a} \frac{a}{x^2} dx + Gmb \int_a^{l+a} dx$$

$$= Gm \left[ \frac{1}{x} \right]_a^{l+a} + Gmb [l]$$

$$= Gm \left[ \frac{1}{l+a} - \frac{1}{a} \right] + Gmb [l]$$



84.  $I = \frac{3}{4} I_0$

$$I_0 \cos^2(d/2) = \frac{3}{4} I_0$$

$$\cos(d/2) = \frac{\sqrt{3}}{2}$$

$$(d/2) = 30^\circ$$

$$d = 60^\circ = \frac{p}{3} \quad \Delta x = \frac{\lambda}{6}$$

As it is formed between 5<sup>th</sup> maxima and 6<sup>th</sup> minima

$Dx \otimes$

$$5l + \frac{1}{6} = \frac{3l}{6}$$

$$\frac{3l}{6} = (m_2 - m_1) \lambda$$

$$t = \frac{3l}{3(m_2 - m_1)} \text{ substituting } t = 9.3 \mu\text{m}$$

85. When separation occurs

$$mg = m\omega^2 r$$

$$g = w^2 r$$

$$r = \frac{g}{w^2}$$

$$T = 1 \text{ sec}, w = 2\pi$$

$$r = \frac{g}{4\pi^2} = \frac{1}{4} = 0.25 \text{ m}$$

86. surfacetensional force = wt. of the liquid column

$$2\pi r d_1 + d_2 \frac{\Delta h}{\rho} = \pi r d_2 - d_1 \frac{\Delta h}{\rho} \rho g$$

$$h = \frac{4T}{(d_2 - d_1) \rho g}$$

87.  $4\pi R^2 x r = \frac{4}{3} \pi R^3 (r_w)$

$$x r = \frac{R}{3} \quad (r_w = 1)$$

$$x = \frac{R}{3r}$$

88.  $h = \frac{r^2 w^2}{2g} = \frac{25 \times 10^{-4} \times (2 \times 2\pi)^2}{2 \times 10} \text{ m} = 0.02 \text{ m}$

89.  $T = \frac{2m_1 m_2 g}{m_1 + m_2} \quad S = \frac{T}{\rho r^2}$

$$= \frac{2 \cdot m \cdot 2mg}{3m}$$

$$r = \sqrt{\frac{T}{\rho S}}$$

$$r = \sqrt{\frac{4mg}{3\rho S}}$$

90. Stopping potential 1.1V

i.e.  $KE_{\text{max}} = 1.1 \text{ eV}$

$$h\nu = w_0 + KE_{\text{max}} \quad 1 = 4000 \text{ \AA}$$

$$\frac{12400}{4000} = w_0 + 1.1 \text{ eV} \quad w_0 = 2 \text{ eV}$$

$$\lambda_0 = \frac{12400}{2} = 6200 \text{ \AA} = 620 \text{ nm}$$